

Microsimulation of Urban Development and Location Choices: Design and Implementation of UrbanSim

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Abstract

UrbanSim is a new urban simulation model, developed over the past several years, which is now operational in three urban areas in the United States. The model system is designed to address emerging needs to better coordinate transportation and land use planning as a result of recognition of the strong interactions between land use and transportation, increasing pressure from federal transportation and environmental legislation, and growing adoption of state growth management programs. The model system is implemented as a set of interacting model components that represent the major actors and choices in the urban system, including household moving and residential location, business choices of employment location, and developer choices of locations and types of real estate development, all subject to the influence of governmental transportation and land use policy scenarios. The model design is unusual in the degree of disaggregation of space, time, and agents, and in the adoption of a dynamic disequilibrium approach. The objective of this paper is to describe the entire system at a sufficient level of detail to convey the key specification and design choices made in implementing the system.

1 Introduction

Transportation models have been in routine use by metropolitan planning organizations for decades. However, land use planning is often not well integrated with transportation planning, despite their strong interactions. Further, the state of common practice in land use modeling, and integrated land use and transportation modeling, is much less advanced than that for transportation modeling alone. Some metropolitan regions do no land use modeling at all. Others typically use a simple, aggregate model, which is insensitive to important policy choices regarding zoning, urban growth boundaries, and taxes and incentives. The unfortunate consequence is that the models are then useless for comparing alternate scenarios involving such policy alternatives.

Considerable progress has recently been made in addressing this lack. Over the past several years, we have been designing and evolving a reusable land use modeling system, named UrbanSim [10, 12, 13], which has also been integrated with a range of transportation models. This paper describes version 1.0 of UrbanSim [15], released as Open Source software at <http://www.urbansim.org>. UrbanSim has evolved from a prototype software system and model application tested in Eugene-Springfield, Oregon, to a second-generation production software architecture that has now been used to implement several versions of the

core model components, and has been subsequently applied in Honolulu, Hawaii and Salt Lake City, Utah.

UrbanSim differs from other operational urban models in several prominent characteristics. The first major design difference is that it takes a dynamic disequilibrium approach, representing adjustment processes that occur at different rates, unlike the cross-sectional equilibrium approach taken in models such as DRAM/EMPAL [11], MEPLAN [5], or TRANUS [2]. The assumptions underlying equilibrium models are drawn from general equilibrium in economics, where the focus is on the analytical insight gained by comparing two steady state conditions in perfectly competitive markets that differ only as a result of some exogenous shock to the system. Equilibrium analysis in economics is based on assumptions of perfectly competitive markets, requiring that the actions of any individual cannot affect prices, the products of all firms in the market are homogeneous, resources are perfectly mobile (no transaction costs or delays), and present and future prices and costs are perfectly known to all market participants. Moreover, equilibrium requires that the agendas of all buyers and sellers in all markets be coordinated simultaneously. When considering the complex interactions among urban housing, labor and transportation markets, these assumptions are clearly over-simplifications.

There are at least three different time scales that are relevant to the interacting system of land use and transportation that raise serious concern about the appropriateness of full equilibration. First, travel behavior may change within the scope of a single day, in response to changes in the transport system. Let us call this the short-term. Second, household and business location choices require somewhat longer to make adjustments to transport system changes, so that even if we ignore the transaction costs of moving and the lack of perfect information, we cannot expect location demand to equilibrate to transport system changes in the short-term. Let us call the location choice adjustment the mid-term. Third, real estate developers will respond speculatively to transport system changes and directly to observed shifts in demand for locations, over yet a longer time frame of several years that is required by the time to assemble land and financing, develop plans and obtain permits, extend infrastructure, and of course, prepare a site and construct buildings. We refer to the multiple-year time scale for the real estate development process as the long-term.

One might suggest that the time scales are irrelevant if we get the same outcome in the long run, after all the adjustments are accounted for. This is unlikely for several reasons. Consider that during the time frame that a developer is constructing real estate, processes that occur in the short and mid-term are changing, so that decisions made at the beginning of the real estate development process are made sub-optimal by these changes, resulting in the patterns of over- and under-building so common in urban real estate markets. Moreover, committed development, even if misguided and suboptimal, is durable, and influences prices and availability of real estate opportunities for households and firms and competing developers, making path-dependence an important part of the reaction to a transport system change. And of course, we know that relocation decisions are constrained by many factors, so that a change in transportation costs due to a transport system or pricing change are unlikely to be large enough to cause every household and business to relocate to an 'optimal' location with respect to balancing transportation and other costs, in the way that full equilibration requires.

So, if we impose congestion pricing, or open a new highway or rail system, in year 2010, why should we expect that the real estate demand and supply would be able to respond in the short-term of that given year, in the way that a full equilibration of transportation and land use would suggest? It might make more sense to identify the relevant time scales of these three processes, and assess the degree to which partial equilibration occurs, as a function of the rate of adjustment of the process. This is the approach we have taken in the design of UrbanSim.

Second, the model differs from prior modeling efforts by taking an extremely disaggregate approach, modeling individual households, jobs, and real estate development and location choices using grid cells of 150×150 meters in size. The model inputs include address-level business establishment data, and parcel level land use and real estate inventories. The model system microsimulates the annual evolution in locations of individual households and jobs, and the evolution of the real estate within each individual grid cell as the result of actions by real estate developers. To our knowledge, no other model system to date has been operationalized at this level of detail in time, space, and agents.

Third, the model system is implemented within a software architecture that has been specifically designed to support disaggregate spatial simulation using a modular approach to the management of data and model components. The software is written in Java, and has been developed as an Open Source project using the GNU General Public Licence [7], which means that anyone can freely access the source code, modify it, and redistribute it. The aim of this approach is simultaneously to encourage collaboration, improve the openness and transparency of the model system, and increase the robustness and speed of evolution of the software and model system. The Open Source approach to software development, perhaps the best known example of which is the Linux operating system, has been increasingly adopted as a viable and competitive approach, as compared to proprietary systems. Our hope is that access to the model without proprietary restrictions will stimulate rapid innovation in an area that is in significant need of new approaches, and where research funds for new development are limited.

These design choices were motivated by the need to address policy questions that require substantial geographic detail and a level of behavioral realism inconsistent with general equilibrium assumptions, within a policy process that is increasingly open to public scrutiny and participation. Recent reviews of these and other models can be found elsewhere [4, 6, 9]. We review briefly in the next section the software architecture, and then move to a description of the current model specifications as applied in Eugene-Springfield. The paper concludes with an assessment of the current state of the system and plans for its evolution.

2 Software Architecture

The UrbanSim software architecture has four principal components:

1. *models* that encode the behavior of agents in the simulation (such as households and developers), as well as the objects they operate upon (such as land parcels and buildings),
2. a *model coordinator* that schedules models to run and notifies them when data of interest has changed,
3. an *object store* that holds the shared representations of agents and other entities in the simulated world, and
4. a *translation and aggregation layer* that performs a range of data conversions to mediate between the object store and the models.

Models represent different actors or processes in the urban environment. In addition to encapsulating the behavior of the actor or process, each model is also responsible for defining the set of object types it operates on, and the fields of those objects with which it is concerned. A model can specify that it wishes to share fields also declared by other models, thus providing one technique for data-level coupling and integration of models via the object store. A model can also declare new object types that encapsulate domain-specific data not previously declared (e.g., a water quality model might declare a nutrient load value). A model may specify a set of object types and fields it wishes to monitor for updates, creations, or deletions. Each model is also responsible for indicating how frequently it wishes to be executed; there are no external constraints on how frequently or regularly a model need run.

The models do not communicate directly with each other; rather, they communicate via shared data held in the object store, mediated by the translation and aggregation layer. This extensible, modular architecture supports system evolution, in particular replacing a model with a revised one, and creating and integrating new models. It allows models to define and share common sets of objects that they all operate upon, via the object store (regardless of the original source of the data), and also allows them to monitor changes to data fields, providing a convenient method for models to synchronize their actions. Lastly, it provides the Translation/Aggregation Layer that automatically performs a range of data conversions that facilitate model integration. For example, models can query for zonal population totals. The Translation/Aggregation Layer computes and maintains these totals independent of the information in the object store, which consists of population information at the grid cell level.

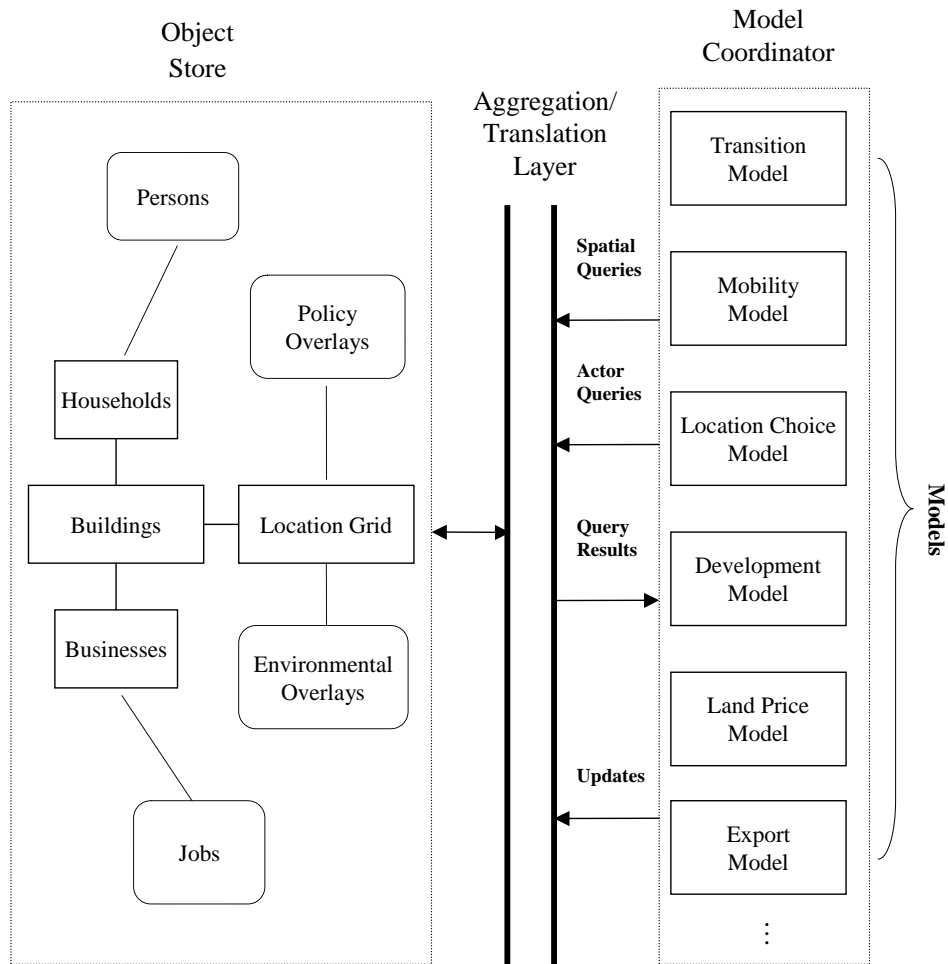


Figure 1: UrbanSim architecture

A primary goal of this architecture is to move as much of the software complexity out of the individual models and into the supporting infrastructure as possible. This supporting infrastructure need be written just once, and can have the attention of an expert programmer. The models, on the other hand, are both numerous and frequently changing. Often, specifying them is a complex process, involving considerable domain-specific knowledge and testing; the more one can relieve the model writers of programming burdens the better, so that they can concentrate on issues arising from the domain.

3 Model Structure

UrbanSim takes several key inputs as exogenous. Two of these are from external model systems: a macroeconomic model to predict future macroeconomic conditions such as population and employment by sector, and a travel demand model system to predict travel conditions such as congested times and composite utilities of travel between zones. The latter is loosely coupled to UrbanSim, with land use predictions input to the external travel models, and travel conditions input to subsequent annual iterations of the UrbanSim land use model system.

UrbanSim normally schedules each model to operate once per simulated year, with the data flow as shown in Figure 2. The data store contains the current state of all objects in the system, with archiving as needed by individual models, or as requested by the user into files for processing by external tools (such as GIS systems). Each of the key models is described in the following subsections. The mathematical structure of the underlying procedures in the model are virtually identical for the household and employment models, so for brevity the household equations are omitted from the presentation below.

The system reads exogenous inputs not only from external macroeconomic and travel demand models, but also from user input. These user inputs include assumptions reflecting land use policies that regulate real estate development, and any user-specified events that describe scheduled events representing changes in employment, real estate development or land policy the user intends to apply to the model in a simulation year beyond the initial or base year.

The main model components, in the order of their execution in a given simulated year, are the economic and demographic transition models, the household and employment mobility models, the accessibility model, the household and employment location choice models, the real estate development model, and the land price model. An output module writes simulation results in user-specified formats to output files for further analysis or processing, such as by travel demand models or by GIS. (For software engineering reasons, the output module is implemented as a model, namely the Export Model. Conceptually, however, it is not a model in the same sense as the others, since it is not an actor or process in the urban environment, but just reads information and exports it to external files.)

Locations in the model are based on a grid with a resolution of 150×150 meters per grid cell. Cells are cross-referenced to Traffic Analysis Zones for indexing travel model outputs, and to city, county, and other geographic overlays for indexing land use policies that apply to specific jurisdictions or overlays.

3.1 Accessibility Model

Since this model is not of the monocentric or spatial interaction genre, in which the choice of workplace is exogenous and residential locations are chosen on the basis principally of commute to the city center or to a predetermined workplace, we deal with accessibility in a more general framework. Accessibility is considered a normal good, like other positive attributes of housing, on which consumers place a positive economic value. We therefore expect that consumers value access to workplaces and shopping opportunities, among the many other attributes they consider in their housing preferences. However, not all households respond to accessibility in the same way. Retired persons would be less influenced by accessibility to job opportunities than would working age households, for instance.

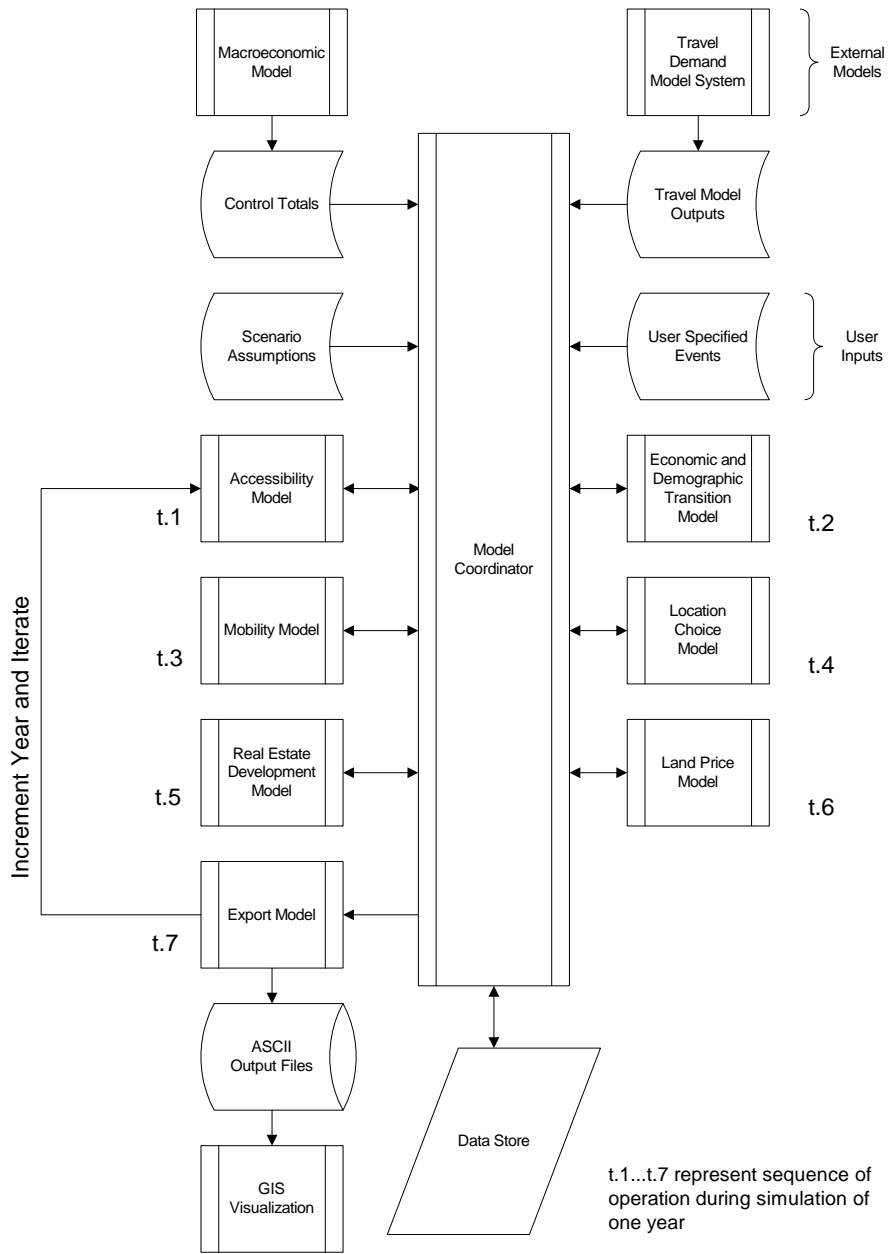


Figure 2: UrbanSim Data Flow

We operationalize the concept of accessibility for a given location as the distribution of opportunities weighted by the composite utility of all modes of travel to those destinations, defined as the logsum from the mode choice model for each origin-destination pair. The resulting access measure A_i for each location i is thus:

$$A_i = \sum_{j=1}^J D_j e^{L_{aij}} \quad (1)$$

where:

D_j is the quantity of activity in location j
 L_{aij} is the composite utility, or logsum, for households with vehicle ownership level a from location i to location j

The accessibility model reads the logsum matrix from the travel model and the land use distribution for a given year, and creates accessibility indices for use in the household and business location choice models. The general framework is to summarize the accessibility from each zone to various activities for which accessibility is considered important in household or business location choice.

Since UrbanSim operates annually, but travel model updates are likely to be executed for only two to three of the years within the forecasting horizon, travel utilities remain constant from one travel model run until they are replaced by the next travel model result. Although travel utilities remain constant between years for which the travel model system is applied, the activity distribution in these accessibility indices is updated annually, so that the accessibility indices change from one year to the next to reflect the evolving spatial distribution of activities. There is considerable disagreement in the literature about how or whether land use and transportation should be brought to equilibrium through multiple iterations of the land use and transportation models. As discussed in the introduction to the paper, however, there is little basis for assuming that the effects of major transportation projects such as rail or highway systems should instantaneously generate their full effects on land use. In reality, land use is likely to respond to transportation improvements over several years or even decades, depending on the magnitude of the change. As a result, we do not propose any within-year iteration between the land use and transportation models, and only propose applying the travel models as needed to reflect system changes, or sufficient land use change to generate significant differences in congestion patterns.

3.2 Economic and Demographic Transition Models

3.2.1 Economic Transition Model

Employment is classified by the user into employment sectors based on aggregations of Standard Industrial Classification codes. Typically 10 to 20 sectors are defined, based on the local economic structure. Aggregate forecasts of economic activity and sectoral employment are exogenous to UrbanSim, and are used as inputs to the model. These forecasts may be obtained from state economic forecasts or from commercial or in-house sources.

The Economic Transition Model integrates these exogenous forecasts of aggregate employment by sector with the UrbanSim database by computing the sectoral growth or decline from the preceding year, and either removing jobs from the database in sectors that are declining, or creating and queuing jobs to be placed in the employment location choice model for sectors that experience growth. If the user supplies only total employment control totals, rather than totals by sector, the sectoral distribution is assumed consistent with the current sectoral distribution. In cases of employment loss, the probability that a job will be removed is assumed proportional to the spatial distribution of jobs in the sector. The jobs that are removed vacate the space they were occupying, and this space becomes available to the pool of vacant space for other jobs

to occupy in the location component of the model. This procedure keeps the accounting of land, structures, and occupants up to date.

New jobs are not immediately assigned a location. Instead, new jobs are added to the database and assigned a null location, to be resolved by the Employment Location Choice Model (Section 3.4.1). The model proceeds as follows.

Calculate the number of jobs to be added or removed (a scalar). Here $|J_{s(t-1)}|$ indicates the number of elements in (cardinality of) the set $J_{s(t-1)}$.

$$\Delta J_{st} = C_{st} - |J_{s(t-1)}| \quad (2)$$

where:

- ΔJ_{st} is the change from year $t - 1$ to t in total jobs in sector s ,
- C_{st} is the exogenous total employment in sector s in year t ,
- $J_{s(t-1)}$ is the set of all jobs in sector s in year $t - 1$.

J_{st} is either the union of the previous year's jobs and some newly created jobs, or the difference between the previous year's jobs and some number of jobs to remove.

$$J_{st} = \begin{cases} J_{s(t-1)} \cup F_{st}, & \text{if } \Delta J_{st} > 0 \\ J_{s(t-1)}, & \text{if } \Delta J_{st} = 0 \\ J_{s(t-1)} - F_{st}, & \text{if } \Delta J_{st} < 0 \end{cases} \quad (3)$$

and

$$J_{st} \subset J_A \quad (4)$$

where:

- J_{st} is the set of all jobs in sector s at time t ,
- F_{st} is the set of jobs in flux in sector s in year t ,
- J_A is the universe of jobs.

The jobs in flux are jobs being added or removed from this sector at this time. If we are adding jobs, new jobs are taken from the universe of all jobs and added to the set of jobs present in the model at time t . If we are removing jobs, the flux jobs are a random subset of the current jobs of a particular sector in the model.

$$F_{st} = \begin{cases} \{j \in J_A \mid j \notin J_{st}, j \text{ is in sector } s\}, & \text{if } \Delta J_{st} > 0 \\ \emptyset, & \text{if } \Delta J_{st} = 0 \\ \{j \in J_{st}\}, & \text{if } \Delta J_{st} < 0 \end{cases} \quad (5)$$

subject to

$$|F_{st}| = |\Delta J_{st}|. \quad (6)$$

(Equation 6 above constrains the cardinality of the set of flux jobs to be equal to the absolute value of the change in number of jobs.)

Let U_t be the set of jobs that do not have a location match at time t . For the base year $t = 0$, U_t will initially be the empty set; in subsequent years it will initially be the remaining unplaced jobs from the previous year (although typically this will be the empty set as well).

$$U_t \leftarrow \begin{cases} \emptyset & \text{if } t = 0 \\ U_{t-1} & \text{otherwise} \end{cases} \quad (7)$$

If we are adding new jobs then they are initially without a location. They are added to the set of unplaced jobs and will be subsequently placed by the Employment Location Choice Model.

$$\text{for each sector } s: \quad \text{if } \Delta J_{st} > 0 \text{ then } U_t \leftarrow U_t \cup F_{st} \quad (8)$$

If we are removing jobs then we need to remove the corresponding placed jobs pairs.

$$\text{for each sector } s: \quad \text{if } \Delta J_{st} < 0 \text{ then } P_t \leftarrow P_t - \{ (j, l) \in P_t \mid j \in F_{st} \} \quad (9)$$

where:

P_t is the set of all pairs (j, l) representing a job j placed at location l at time t .

Also, the locations previously occupied by the jobs being removed must be placed in the set of vacant locations.

$$V_t = \{ l \in L_t^J \mid \forall j \in J_t (j, l) \notin P_t \} \quad (10)$$

where:

V_t is the set of locations that do not have a job match at time t ,
 L_t^J is the set of all locations at time t where a job could be placed,
 J_t is the set of jobs at time t .

3.2.2 Demographic Transition Model

The Demographic Transition Model accounts for changes in the distribution of households by type over time, using an algorithm analogous to that used in the Economic Transition Model. In reality, these changes result from a complex set of social and demographic changes that include aging, household formation, divorce and household dissolution, mortality, birth of children, migration into and from the region, changes in household size, and changes in income, among others. The data (and theory) required to represent all of these components and their interactions adequately are not readily available. Instead, the Demographic Transition Model, like the Economic Transition Model described in Section 3.2.1, uses external control totals of population and households by type (the latter only if available) to provide a mechanism for the user to approximate the net results of these changes. Analysis by the user of local demographic trends may inform the construction of control totals with distributions of household size, age of head, and income. If only total population is provided in the control totals, the model assumes that the distribution of households by type remains static.

As in the economic transition case, household births are added to a list of movers that will be located by the Household Location Choice Model. Household deaths, on the other hand, are accounted for in this model by removing those households from the housing stock, and by properly accounting for the vacancies created by their departure. The demographic transition model is analogous in form to the employment transition model described above.

3.3 Mobility Models

3.3.1 Employment Mobility Model

Employment mobility and location choices are made by firms. However, in the current version of UrbanSim, we use individual jobs as the units of analysis. This is equivalent to assuming that businesses are making individual choices about the location of each job, and are not constrained to moving an entire establishment. A prior version of the employment location model used the business establishment as the unit of analysis. While there are advantages to each approach, the main advantage to using the individual job as the unit of analysis is that it affords greater capacity for modeling the location of jobs in large businesses.

The Employment Mobility Model predicts the probability that jobs of each type will move from their current location or stay during a particular year. This is a transitional change that could reflect job turnover by employees, layoffs, business relocations, or closures. Similar to the economic transition model when handling job losses in declining sectors, the model assumes that the probability of moving is proportional to the spatial distribution of jobs in the sector. All placement of jobs is managed through the employment location model.

As in the case of job losses predicted in the economic transition component, the application of this model requires subtracting jobs by sector from the buildings they currently occupy, and noting this space as vacant. These job counts are added to the unallocated new jobs by sector calculated in the economic transition model. The combination of new and moving jobs serve as a pool to be located in the employment location choice model. Vacancy of nonresidential space is then updated, making space available for allocation in the employment location choice model.

Since it is possible that the relative attractiveness of commercial space in other locations when compared with an establishment's current location may influence its decision to move, an alternative structure for the mobility model could use the marginal choice in a nested logit model with a conditional choice of location. In this way, the model would use information about the relative utility of alternative locations compared to the utility of the current location in predicting whether jobs will move. While this might be more theoretically appealing than the specification given, it is generally not supported by the data available for calibration. Instead, the mobility decision is treated as an independent choice, and the probabilities estimated by annual mobility rates directly observed over a recent period for each sector. These rates are computed from longitudinally linked business establishment files, if available.

The resulting form of the employment mobility model is as follows. M_{st} is a set of jobs that are chosen to be moved based on $P(j, t)$, a Monte Carlo sampling process using the annual mobility rate for sector s . This procedure generates a random number between 0 and 1, and compares it to the cumulative probability of each possible outcome. The selected outcome is then the one that has a cumulative probability interval which contains the random number. In the case of only two outcomes, such as the mobility prediction, the procedure simplifies to an evaluation of whether the random number is greater than the mobility probability, in which case the move outcome is chosen.

$$M_{st} = \{j \in J_{st} \mid P(j, t)\}, \quad (11)$$

where:

M_{st} is the set of jobs in sector s at time t that are uprooted by the mobility model,
 $P(j, t)$ is a Monte Carlo sampling process determining if job j will be moved at time t .

The jobs to be moved are now unplaced, and so are added to the unplaced jobs set:

$$\text{for each sector } s: U_t \leftarrow U_t \cup M_{st} \quad (12)$$

and are removed from the job location pairs set:

$$\text{for each sector } s: P_t \leftarrow P_t - \{(j, l) \in P_t \mid j \in M_{st}\}. \quad (13)$$

Finally, the locations previously occupied by the jobs being moved must be added to the set of vacant locations:

$$V_t = \{l \in L_t^J \mid \forall j \in J_t (j, l) \notin P_t\}. \quad (14)$$

3.3.2 Household Mobility Model

The Household Mobility Model is similar in form to the Employment Mobility Model described above. The same algorithm is used, but with rates or coefficients applicable to each household type. For households, mobility probabilities are estimated from the Census Current Population Survey, which provides a national database on which annual mobility rates are computed by type of household. This will reflect differential mobility rates for renters and owners, and households at different life stages.

Application of the Household Mobility Model requires subtracting mover households by type from the housing stock by cell, and adding them to the pool of new households by type estimated in the Demographic Transition Model. The combination of new and moving households serves as a population of households to be located by the Household Location Choice Model. Housing vacancy is updated as movers are subtracted, making the housing available for occupation in the household location and housing type choice model.

3.4 Location Choice Models

3.4.1 Employment Location Choice Model

In this model, we predict the probability that a job that is either new (from the Economic Transition Model), or has moved within the region (from the Employment Mobility Model), will be located at a particular site. The grid cells used as the basic geographic unit of analysis in the current model implementation contain variable quantities of space to be occupied by jobs. The number of available job locations within a grid cell will depend mainly on the total square footage of nonresidential floorspace in the cell, and on the density of the use of space (square feet per employee). Given the possibility that some jobs will be located in residential units, however, housing as well as nonresidential floorspace must be considered in job location. We have defined a maximum rate of home-based employment, determined using local data for a particular metropolitan region, to identify the potential set of spaces available for home-based employment. The set of job locations available for placing a job, then, are the union of the spaces in nonresidential floorspace and a subset of the residential units in the cell:

$$|L_t^J| = \frac{s_l}{r_{sd}} + \frac{h_l}{r_{hd}} \quad (15)$$

where:

- s_l is a scalar representing the total nonresidential square footage of floorspace in location l ,
- h_l is a scalar representing the total number of housing units in location l ,
- r_{sd} is a space utilization rate for nonresidential space for devtype d (sqft per employee),
- r_{hd} is a home-based employment rate, defined as the minimum units per job for devtype d

For both the employment location and household location models, we take the stock of available space as fixed in the short run of the intra-year period of the simulation, and assume that locators are price takers. That is, a single locating job or household does not have enough market power to influence the transaction price, and must accept the current market price as given.

The variables included in the employment location choice model are drawn from the literature in urban economics. We expect that accessibility to population, particularly high-income population, increases bids

for retail and service businesses. We also expect that two forms of agglomeration economies influence location choices: localization economies and inter-industry linkages.

Localization economies represent positive externalities associated with locations that have other firms in the same industry nearby. The basis for the attraction may be some combination of a shared skilled labor pool, comparison shopping in the case of retail, co-location at a site with highly desirable characteristics, or other factors that cause the costs of production to decline as greater concentration of businesses in the industry occurs. The classic example of localization economies is Silicon Valley. Inter-industry linkages refer to agglomeration economies associated with location at a site that has greater access to businesses in strategically related, but different, industries. Examples include manufacturers locating near concentrations of suppliers in different industries, or distribution companies locating where they can readily service retail outlets.

One complication in measuring localization economies and inter-industry linkages is determining the relevant distance for agglomeration economies to influence location choices. At one level, agglomeration economies are likely to affect business location choices between states, or between metropolitan areas within a state. Within a single metropolitan area, we are concerned more with agglomeration economies at a scale relevant to the formation of employment centers. The influence of proximity to related employment may be measured using two scales: a regional scale effect using zone-to-zone accessibilities from the travel model, or highly localized accessibilities using radial queries of the area immediately around the given grid cell. Most of the spatial queries used in the model are of the latter type, because the regional accessibility variables tend to be very highly correlated with each other, and because agglomerations are expected to be very localized. (The use of radial queries surrounding grid cells also avoids the problems of arbitrary zonal aggregations.)

Age of buildings is included in the model to estimate the influence of age depreciation of commercial buildings, with the expectation that businesses prefer newer buildings and discount their bids for older ones. This reflects the deterioration of older buildings, changing architecture, and preferences, as is the case in residential housing. There is the possibility that significant renovation will make the actual year built less relevant, and we would expect that this would dampen the coefficient for age depreciation. We do not at this point attempt to model maintenance and renovation investments and the quality of buildings.

Density, the inverse of lot size, is included in the location choice model. We expect businesses, like households, to reveal different preferences for land based on their production functions and the role of amenities such as green space and parking area. As manufacturing production continues to shift to more horizontal, land-intensive technology, we expect the discounting for density to be relatively high. Retail, with its concentration in shopping strips and malls, still requires substantial surface land for parking, and is likely to discount bids less for density. We expect service firms to discount for density the least, since in the traditional urban economics models of bid-rent, service firms generally outbid other firms for sites with higher accessibility, land cost, and density.

We might expect that certain sectors, particularly retail, show some preference for locations near a major highway, and are willing to bid higher for those locations. Distance to a highway is measured in meters, using grid spatial queries. We also test for the residual influence of the classic monocentric model, measured by travel time to the CBD, after controlling for population access and agglomeration economies. We expect that, for most regions, the CBD accessibility influence will be insignificant or the reverse of that in the traditional monocentric model, after accounting for the more general measure of access to employment or population, and other effects.

Calibration of the model is based on a geocoded establishment file (matched to the parcel file to link employment by type to land use by type). The model is estimated using a random sample of alternative locations, which has been shown to provide consistent estimates of the coefficients [1]. A sample of geocoded jobs in each sector is used to estimate the coefficients of the location choice model. As with the Household Location Choice Model, the application of the model produces demand by each employment type for cell locations.

The employment location model processes each job in the mover queue in random order, and queries grid cells for alternative locations to consider. These alternatives are sampled in proportion to the capacity of the

built space in the cell for accommodating jobs. The number of alternatives to consider may be determined by the user. Jobs may be located in housing units, as is increasingly the case with home-based employment through telecommuting and small independent home-based businesses. A logit model is applied to estimate the probability that the current job will move to each of the alternative job spaces under consideration. Monte Carlo simulation is used to generate a decision to locate in a particular alternative, and once this choice is made, the job is assigned to the cell, and the respective quantities of vacant and used space in the cell are updated. Once a job space been chosen and occupied by a locating job, it becomes unavailable for consideration by remaining jobs in the mover queue.

The independent variables used in the employment location choice model can be grouped into the categories of real estate characteristics, regional accessibility, and urban-design scale effects as shown below:

- Real Estate Characteristics
 - Prices*
 - Development type (land use mix, density)*
- Regional accessibility
 - Access to population*
 - Travel time to CBD, airport*
- Urban design-scale
 - Proximity to highway, arterials*
- Local agglomeration economies within and between sectors: center formation

Using these independent variables, the employment location model is specified as a multinomial logit model, with separate equations estimated for each employment sector. The model proceeds as follows.

The job location pairs set contains all pairs of placed jobs and their locations.

$$P_t = \{ (j, l) \mid j \in J_t, l \in L_t^J, \text{job } j \text{ is placed at location } l \}, \quad (16)$$

$$U_t = \{ j \mid j \in J_t, \forall l \in L_t^J (j, l) \notin P_t \}, \quad (17)$$

$$V_t = \{ l \mid l \in L_t^J, \forall j \in J_t (j, l) \notin P_t \}, \quad (18)$$

$$D_{st} = \{ (l, p) \mid l \in V_t, p \text{ is the probability of a job in sector } s \text{ locating in } l \} \quad (19)$$

where:

D_{st} is the set of pairs representing the probability of an employee of sector s locating to a particular location at time t .

Monte Carlo sampling of the location choices for each sector occurs over the distribution given by D_{st} .

$$F_t = \{ (j, l) \mid j \in U_t, \text{Monte Carlo choice of } l \text{ from } D_{st} \text{ given the sector of } j \}, \quad (20)$$

where:

F_t is the set of new job/location pairs created using a Monte Carlo sampling from D_{st} for each sector.

The cardinality of the set of new job/location pairs is constrained to be equal to the cardinality of the set of unplaced jobs or of the set of unoccupied locations, whichever is smaller.

$$|F_t| = \min(|U_t|, |V_t|). \quad (21)$$

Finally, the set of job/location pairs is modified to reflect the new matchings, the placed jobs are removed from the set of unplaced jobs, and the newly occupied locations are removed from the set of vacant locations.

$$P_t \leftarrow P_t \cup F_t \tag{22}$$

$$U_t \leftarrow U_t - \{j \in U_t \mid \exists l (j, l) \in F_t\} \tag{23}$$

$$V_t \leftarrow V_t - \{l \in V_t \mid \exists j (j, l) \in F_t\} \tag{24}$$

3.4.2 Household Location Choice Model

In this model, as in the employment location model, we predict the probability that a household that is either new (from the transition component), or has decided to move within the region (from the mobility component), will choose a particular location defined by a grid cell. As before, the form of the model is specified as multinomial logit, with random sampling of alternatives from the universe of available (vacant) housing units, including those units vacated by other movers in the current year.

The model architecture allows location choice models to be estimated for households stratified by income level, the presence or absence of children, and other life cycle characteristics. Alternatively, these effects can be included in a single model estimation through interactions of the household characteristics with the characteristics of the alternative locations. The current implementation is based on the latter, but is general enough to accommodate stratified estimation, for example by household income. The variables used in the model are drawn from the literature in urban economics, urban geography, and urban sociology. An initial feature of the model specification is the incorporation of the classical urban economic trade-off between transportation and land cost. This has been generalized to account not only for travel time to the classical monocentric center, the CBD, but also to more generalized access to employment opportunities and to shopping. These accessibilities to work and shopping are measured by weighting the opportunities at each destination zone with a composite utility of travel across all modes to the destination, based on the logsum from the mode choice travel model.

These measures of accessibility should negate the traditional pull of the CBD, and, for some population segments, potentially reverse it. In addition to these accessibility variables, we include in the model a net building density, to measure the input-substitution effect of land and capital. To the extent that land near high accessibility locations is bid up in price, we should expect that builders will substitute capital for land and build at higher densities. Consumers for whom land is a more important amenity will choose larger lot housing with less accessibility, and the converse should hold for households that value accessibility more than land, such as higher income childless households.

The age of housing is considered for two reasons. First, we should expect that housing depreciates with age, since the expected life of a building is finite, and a consistent stream of maintenance investments are required to slow the deterioration of the structure once it is built. Second, due to changing architectural styles, amenities, and tastes, we should expect that the wealthiest households prefer newer housing, all else being equal. The exception to this pattern is likely to be older, architecturally interesting, high quality housing in historically wealthy neighborhoods. The preference for these alternatives are accommodated through a combination of nonlinear or dummy variable treatment for this type of housing and neighborhood.

A related hypothesis from urban economics is that, since housing is considered a normal good, it has a positive income elasticity of demand. This implies that as incomes rise, households will spend a portion of the gains in income to purchase housing that is more expensive, and that provides more amenities (structural and neighborhood) than their prior dwellings. A similar hypothesis is articulated in urban sociology in which upward social mobility is associated with spatial proximity to higher status households. Both of these hypotheses predict that households of any given income level prefer, all else being equal, to locate in neighborhoods that have higher average incomes. (UrbanSim does not attempt to operationalize the concepts of social status or social assimilation, but does consider income in the location choice.)

The age hypothesis and the two income-related hypotheses are consistent with the housing filtering model, which explains the dynamic of new housing construction for wealthy households that sets in motion a chain

of vacancies. The vacancy chain causes households to move into higher status neighborhoods than the ones they leave, and housing units to be successively occupied by lower and lower status occupants. At the end of the vacancy chain, in the least desirable housing stock and the least desirable neighborhoods, there can be insufficient demand to sustain the housing stock and vacancies go unsatisfied, leading ultimately to housing abandonment. We include in the model an age depreciation variable, along with a neighborhood income composition set of variables, to collectively test the housing filtering and related hypotheses.

Housing type is included in the model as a set of dummy variables for alternative development types. Development types correspond to the density and land use mix within a cell, with multiple categories of residential development, and mixed use development encompassing both commercial space and residential housing. These are discussed further in Section 3.5 describing the real estate development model.

One of the features that households prefer is a compatible land use mix within the neighborhood. It is likely that residential land use, as a proxy for land uses that are compatible with residential use, positively influences housing bids. On the other hand, industrial land use, as a proxy for less desirable land use characteristics, would lower bids. There is some evidence that mixed use neighborhoods that contain retail and services, in the form advocated by proponents of new urbanist or neotraditional neighborhood design, are positively valued. We test this using the proximity of retail employment within walking distance.

The household location model is estimated using a random sampling of alternative locations, as is the case in the employment location model. In application, each locating household is modeled individually, and a sample of alternative cell locations is generated in proportion to the available (vacant) housing. Monte Carlo simulation is used to select the specific alternative to be assigned to the household, and vacant and occupied housing units are updated in the cell.

The market allocation mechanism used to assign households and jobs to available space, then, is not done through a general equilibrium solution in which consumers and suppliers optimize across all alternatives based on perfect information, and zero transaction costs, with prices on all buildings at each location adjusting to the general equilibrium solution that perfectly matches consumers and suppliers to clear the market. Rather, the solution is based on an expectation of incomplete information (we sample alternatives) and nontrivial transaction and search costs (only a fraction of jobs and households move annually), so that movers attempt to obtain the most satisfactory location from the sampled vacant real estate stock. Prices respond at the end of the year to the characteristics of locations and the balance of demand and supply (vacancy rates) at each location.

The independent variables can be organized into the three categories of housing characteristics, regional accessibility, and urban-design scale effects as shown below.

- Housing Characteristics
 - Prices (interacted with income)*
 - Development types (density, land use mix)*
 - Housing age*
- Regional accessibility
 - Job accessibility by auto-ownership group*
 - Travel time to CBD and airport*
- Urban design-scale (local accessibility)
 - Neighborhood land use mix and density*
 - Neighborhood employment*

3.5 Real Estate Development Model

3.5.1 Data

The real estate developer model simulates the construction of new real estate, either through the construction of new development or the intensification or conversion of existing development. The data is structured as grid cells, currently specified as 150×150 meters in resolution (though this is a specification issue and not a restriction in the software). Parcel data is preprocessed to obtain the intersection of parcels and grid cells, and then to construct a composite representation of the real estate development within each cell. Cells are then classified on the basis of their real estate composition, into ‘Development Types’, as shown in Table 1. The classification is based on the number of housing units in a cell, and the quantity of nonresidential square footage in the cell. Cells containing some housing and almost no nonresidential square footage are considered residential in character. Those containing a diverse mixture of housing and nonresidential floorspace are considered mixed-use, and those cells containing principally nonresidential square footage are further classified into commercial, industrial or governmental types.

The data to estimate the coefficients for the developer model is derived from preprocessing the parcel and grid data, making heavy use of the year built values of the existing development in the assessor records. The data preparation procedure imputes year built values for those records for which it is missing by examining the surrounding cells of the same type and drawing from the distribution of observed values. Once the data is complete, historical development ‘events’ are identified for some user-specified period of time, and these events are extracted to a file for further analysis. Events, within this framework, are any changes in the real estate development within a cell that is identified by examining the year built values within the data. This means that the procedure is capable of identifying any new construction that has a year built occurring within the specified time frame. However, it does not identify events that involve the demolition of buildings at some time in the past, since normally there is no record of such demolished buildings within the current assessor database. This procedure could be augmented with data derived from building demolition and permit records, but that has not been accounted for in the current specification.

The result of this procedure, then, is the production of a set of development events that represent all observed transitions between any pairs of development types within each year of the specified historical time frame. The time slice for determining the existence of an event is annual, since this is the limit of the information on the vintage of real estate. Also, some development events may be observed in the data that do not indicate a change of development type, but rather an intensification of use within the range specified in the definition of the development types.

3.5.2 Structure

The developer model is structured to predict the probability within a single simulation year of a grid cell experiencing a development event, and if it does experience such an event, identifying the type of event that is most likely. A multinomial logit model is used to estimate these probabilities. Once these probabilities are estimated for a grid cell, commitment of development is simulated using a Monte Carlo sampling process. Implementation of the development takes place by using a development template to obtain the most likely characteristics of the resulting development project within the cell, including the number of housing units, square feet of commercial, industrial and government space, improvement value, and construction schedule. These commitments are then added to the ‘development event’ queue, to be built (added to the database) as scheduled.

Constraints on development outcomes are included through a combination of user-specified spatial overlays and decision rules about specific types of development allowed in different situations. Each cell is assigned a series of overlays through spatial preprocessing using GIS overlay techniques. These overlays can be used to assign user-specified constraints on the type of development that is allowed to occur within each of these overlay designations. The constraints are indicated as allowed conversions between each land use plan designation and each development type in a file supplied by the user as part of the construction of a

DevType	Name	Units	Sqft	Primary Use
1	R1	1	< 1,000	Residential
2	R2	2 - 4	< 1,000	Residential
3	R3	5 - 9	< 1,000	Residential
4	R4	10 - 14	< 2,500	Residential
5	R5	15 - 21	< 2,500	Residential
6	R6	22 - 30	< 2,500	Residential
7	R7	31 - 75	< 5,000	Residential
8	R8	≥ 76	< 5,000	Residential
9	M1	0 - 9	1,000 - 4,999	Mixed R/C
10	M2	10 - 30	2,500 - 4,999	Mixed R/C
11	M3	10 - 30	5,000 - 24,999	Mixed R/C
12	M4	10 - 30	25,000 - 49,999	Mixed R/C
13	M5	10 - 30	≥ 50,000	Mixed R/C
14	M6	≥ 31	5,000 - 24,999	Mixed R/C
15	M7	≥ 31	25,000 - 49,999	Mixed R/C
16	M8	≥ 31	≥ 50,000	Mixed R/C
17	C1	< 10	1,000 - 24,999	Commercial
18	C2	< 10	25,000 - 49,999	Commercial
19	C3	< 10	≥ 50,000	Commercial
20	I1	< 10	1,000 - 24,999	Industrial
21	I2	< 10	25,000 - 49,999	Industrial
22	I3	< 10	≥ 50,000	Industrial
23	GV	≥ 0	≥ 0	Government
24	VC	0	0	Vacant Dev
25	UN	0	0	Undevelopable

Table 1: Development Types

scenario for simulation. Those conversions that are contained in this file are not considered in the model. This is implemented by eliminating them from the choice set for any cell affected by the constraint. These constraints are therefore interpreted as binding constraints, and not subject to market pressure. Currently, if users wish to examine the impact of these constraints, they would need to relax a particular constraint within one scenario and compare the scenario results to a more restrictive policy. The overlays used in the Eugene-Springfield model application include the following features:

- Land use plan designation
- City
- County
- Wetland designation
- Floodplain/floodway
- Stream or riparian buffer
- High slope areas
- Urban Growth Boundary

The independent variables used in the real estate development model can be organized into categories of site characteristics, urban design-scale effects, regional accessibility, and market conditions, as shown below:

- Site characteristics
 - Existing development characteristics*

Land use plan
Environmental constraints

- Urban design-scale
 - Proximity to highway and arterials*
 - Proximity to existing development*
 - Neighborhood land use mix and property values*
 - Recent development in neighborhood*
- Regional accessibility
 - Access to population and employment*
 - Travel time to CBD, airport*
- Market Conditions
 - Vacancy rates*

Using these variables, the real estate development model simulates the probability of each possible transition from one development type to another, for every cell in the model database. The model proceeds as follows.

$$T = \{ (d_1, d_2) \mid \text{devtype } d_1 \text{ can transition to devtype } d_2 \}, \quad (25)$$

$$T_{lt} = \{ d_2 \mid (d_1, d_2) \in T, l \in L_t, d_1 \text{ is the devtype of } l \}, \quad (26)$$

$$P_{lt} = \{ (d, p) \mid j \in T_{lt}, p \text{ is the probability of transitioning to devtype } d \text{ at location } l \}, \quad (27)$$

where:

- T is the set of valid development type transitions,
- T_{lt} is the set of all valid development type transitions at location l at time t ,
- L_t is the set of all locations at time t ,
- P_{lt} is the set of probabilities of transitioning to a particular development type at location l at time t .

The development type for each location is defined to be the outcome of the chosen transition. One probable transition is one that includes no change.

We can then define the set L_{dt} of location and development type pairs at time t as follows:

$$L_{dt} = \{ (l, d) \mid (d, p) \in P_{lt}, l \in L_t, d \text{ is chosen given a Monte Carlo sampling of } p \} \quad (28)$$

3.6 Land Price Model

UrbanSim uses land prices as the indicator of the match between demand and supply of land at different locations and with different development types, and of the relative market valuations for attributes of housing, nonresidential space, and location. This role is important to the rationing of land and buildings to consumers based on preferences and ability to pay, as a reflection of the operation of actual real estate markets. Since prices enter the location choice utility functions for jobs and households, an adjustment in prices will alter location preferences. All else being equal, this will in turn cause higher price alternatives to become more likely to be chosen by occupants who have lower price elasticity of demand. Similarly, any adjustment in land prices alters the preferences of developers to build new construction of various types and densities.

We make the following assumptions:

1. Households, businesses, and developers are all price-takers, and market adjustments are made by the market in response to aggregate demand and supply relationships. Each responds, therefore, to previous period price information.

2. Location preferences and demand-supply imbalances are capitalized into land values. Building value reflects building replacement costs only, and can include variations in development costs due to terrain, environmental constraints, or development policy.
3. There is a long-term structural vacancy rate for each type of property, and the relationship of current vacancy rates to this long-term vacancy rate influences price adjustments.

Land prices are modeled using a hedonic regression [14] of land value on attributes of the land and its environment, including land use mix, density of development, proximity of highways and other infrastructure, land use plan or zoning constraints, and neighborhood effects. The hedonic regression may be estimated from sales transactions if there are sufficient transactions on all property types, and if there is sufficient information on the lot and its location. An alternative is to use tax assessor records on land values, which are part of the database typically assembled to implement the model. Although assessor records may contain biases in their assessment, they do provide virtually complete coverage of the land (with notable exceptions and gaps for exempt or publicly owned property).

The hedonic regression equation encapsulates interactions between market demand and supply, revealing an envelope of implicit valuations for location and structural characteristics. These relative prices have been documented to be relatively consistent over time, with the acknowledgment that the relative values at specific locations change as their underlying characteristics change [3]. Because the hedonic regression includes variables that are to be maintained as part of the simulation system, these can be used to update relative prices over time.

In addition to these relative prices captured by the hedonic regression, the overall price level within the market for each type of real estate moves over time in response to shifts between supply and demand. These fluctuations can be tied to the relationship between the actual market vacancy rate and the long-term structural vacancy rate. When the current vacancy rate falls below the structural rate, price levels rise, and when the current vacancy rate exceeds the structural level, they fall.

These two effects on prices are combined in the land price model. The estimated hedonic regression equation is used to establish relative prices, and the intercept of the equation is adjusted based on the relative position of the current and structural vacancy rate, as follows:

$$P_{ilt} = \alpha + \delta \left(\frac{V_i^s - V_{it}^c}{V_i^s} \right) + \beta X_{ilt} \quad (29)$$

where:

- P_{ilt} is the price of land per acre of development type i at location l at time t
- V_{it}^c is the current vacancy rate at time t , weighting local and regional vacancy
- V_i^s is the long-term structural vacancy rate
- X_{ilt} is a vector of locational and site attributes
- α , δ and β are estimated parameters

Prices are updated annually, after all construction and market activity is completed. These end-of-year prices are then used as the values of reference for market activities in the subsequent year.

The independent variables influencing land prices can be organized into site characteristics, regional accessibility, urban-design scale effects, and market conditions, as shown below:

- Site characteristics
 - Development type*
 - Land use plan*
 - Environmental constraints*

- Regional accessibility
Access to population and employment
- Urban design-scale
Land use mix and density
Proximity to highway and arterials
- Market Conditions
Vacancy rates

3.7 User-Specified Events

Given our current understanding, no model will be able to simulate accurately the timing, location and nature of major events such as a major corporate relocation into or out of a metropolitan area, or a major development project such as a regional shopping mall. In addition, major policy events, such as a change in the land use plan or in an Urban Growth Boundary, are outside the range of predictions of our simulation. (At least in its current form, UrbanSim is intended as a tool to aid planning and civic deliberation, not as a tool to model the behavior of voters or governments. We want it to be used to say “if you adopt the following policy, here are the likely consequences,” but not to say “UrbanSim predicts that in 5 years the county will adopt the following policy.”)

However, planners and decision-makers often have information about precisely these kinds of major events, and there is a need to integrate such information into the use of the model system. It is useful, for example, to explore the potential effects of a planned corporate relocation by introducing user-specified events to reflect the construction of the corporate building, and the relocation into the region (and to the specific site) of a substantial number of jobs, and examine the cumulative or secondary effects of the relocation on further residential and employment location and real estate development choices. Inability to represent such events, in the presence of knowledge about developments that may be ‘in the pipeline,’ amounts to less than full use of the available information about the future, and could undermine the validity and credibility of the planning process. For these reasons, support for three kinds of events has been incorporated into the system: development events, employment events, and policy events.

The software architecture implements simulated events generated by the model components, each of which are time-stamped to occur at a specified time in the future. The user-specified events leverages this facility of the model coordinator within the software architecture, to scan for user specified events in a series of input files prepared by the user. The user defines events according to a specified format, indicating the cells affected, the date at which the event should occur, and the other relevant attributes of the development, employment, or policy event. The model coordinator implement these events at the beginning of the specified year, prior to generating simulated events in the model components.

4 Conclusion

This paper provides a detailed description of the implementation of version 1.0 of UrbanSim, a land use model system designed to integrate with travel demand models in support of metropolitan land use and transportation planning and growth management. The model system is operational and has been applied in three metropolitan areas in the U.S. When released on the Internet as Open Source software in the second quarter of 2000, it was downloaded over 300 times in countries spread over five continents. The model system is undergoing continuous development, and is available at <http://www.urbansim.org>.

Short term (current year) development of the model system is focusing on:

- Developing a graphical user interface for the model,

- Developing visualization tools for comparing scenario results,
- Developing a software system for data integration and synthesis for applying the model system in other locales using available data,
- Developing a design for an extended model system that integrates household choices of activity and travel pattern, vehicle ownership, job location and residential location, essentially dissolving the artificial distinction between land use and travel demand models.

The longer-term research agenda includes:

- Further developing the software architecture to support multi-agent microsimulation efficiently, and developing a high level model specification language;
- Exploring new model structures and estimation techniques, such as Bayesian networks [8], that may provide greater flexibility in representing the complex choice behavior and interdependence than has been feasible in either random utility maximization or decision heuristic approaches to date;
- Developing new model components representing environmental processes and impacts, including land cover change, water demand, and nutrient emissions.

The UrbanSim project represents a long-term collaborative research agenda to improve the state of the practice in metropolitan land use and transportation planning and growth management, and the results reported here document a significant milestone in this agenda.

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