

Design in Complex Systems: Individual Performance versus System Efficiency

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Outline

1. Mix-game
2. Simulation condition
3. Results and discussion
4. Design in competing complex systems

1. 1 Minority game

Minority game (D. Challet, and Y. C. Zhang, *Physica A* 246, 407(1997))

- N: agent number,
- r: system resource $r = L * N$, $L < 1$
- Agent choice: 0 (buy), or 1 (sell)
- Agent memory length m: used to record competing outcome, i.e. a bit string
- Strategy: a response, i.e., 0 or 1, to each possible bit string which represents the history of competing outcome
- Time horizon T: Agents collect the virtual points for their strategies over the time horizon
- Payoff: agents win if they are in minority group in each competition turn

1.2 Mix-game

1. Traders in financial markets

Trend chasers: who effectively play a majority game;
Fundamentalists: who effectively play a minority game.

2. Mix-game

Agents divided in two groups

Group1: agents play majority game; m_1 , T_1 , N_1

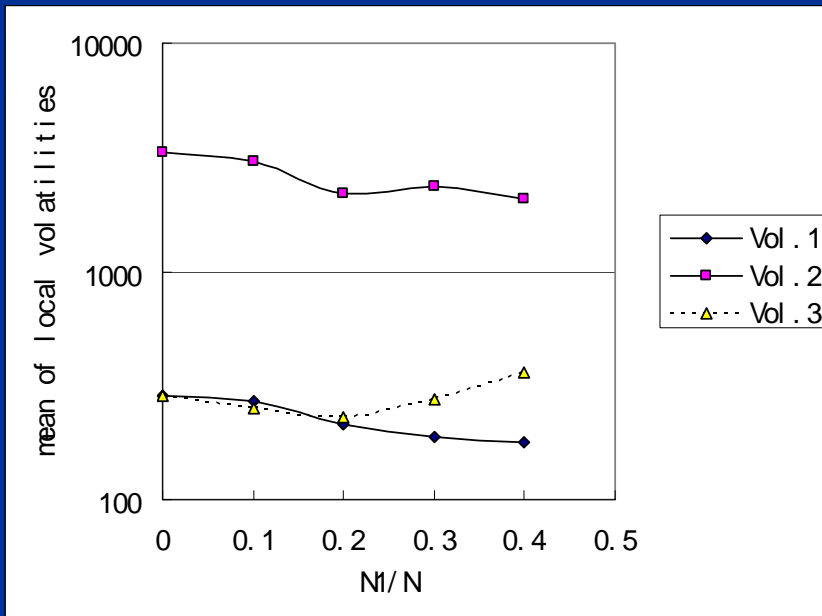
Group2: agents play minority game; m_2 , T_2 , N_2

Total number of agents: $N=N_1+N_2$

2. Simulation condition

- The distribution of initial strategies of agents is randomly uniform in full strategy space (FSS) and remains unchanged during the game.
- Each agent has two strategies, i.e. $s=2$.
- The simulation turns are 3000.
- L is 0.5, i.e. $r = 0.5 * N$.
- $N=201$.

3.1 means of local volatilities vs. different $N1/N$



- Vol.1 : $m1=m2=6$,
 $T1=T2=60$;
- Vol.2 : $m1=6$, $m2=3$,
 $T1=60$, $T2=12$;
- Vol.3 : $m1=3$, $m2=6$,
 $T1=12$, $T2=60$.

3.2 Correlation among R1, R2 and Vol.1

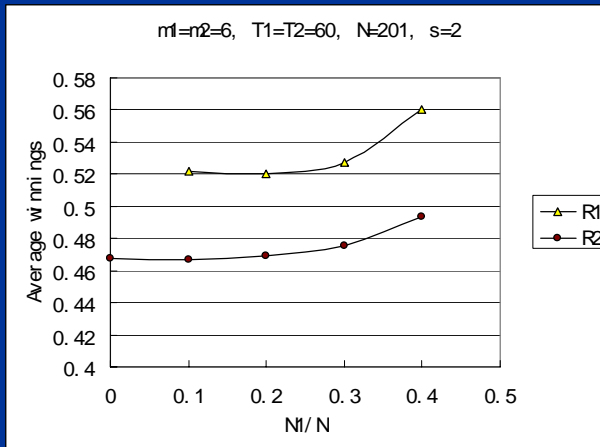
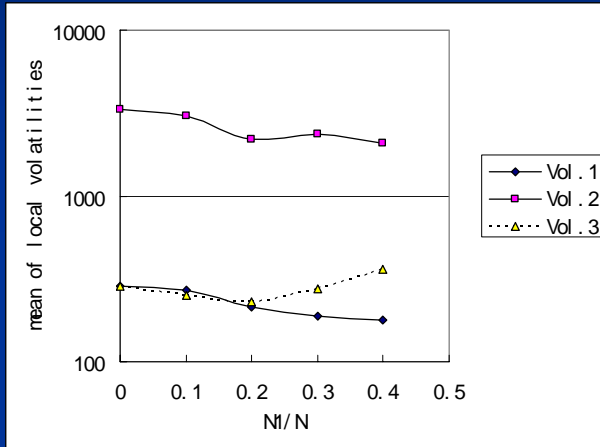


Table 1 correlations of R1, R2 and Vol.1 under the condition of $m1=m2=6$, $T1=T2=60$

Correlation	<i>R1</i>	<i>R2</i>	<i>Vol.1</i>
<i>R1</i>	1		
<i>R2</i>	0.98	1	
<i>Vol.1</i>	-0.63	-0.76	1

Average winnings per agent per turn

3.3 Correlation among R1, R2 and Vol.2

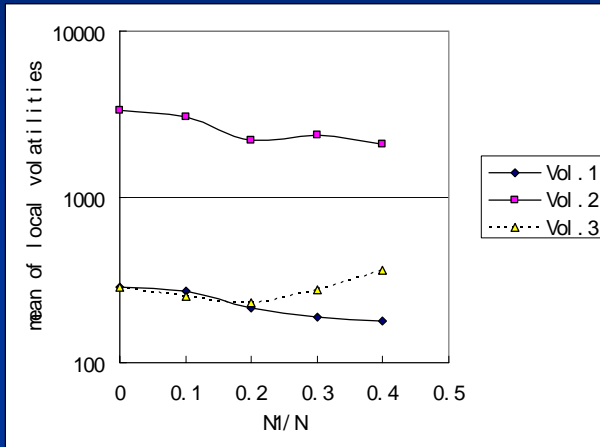
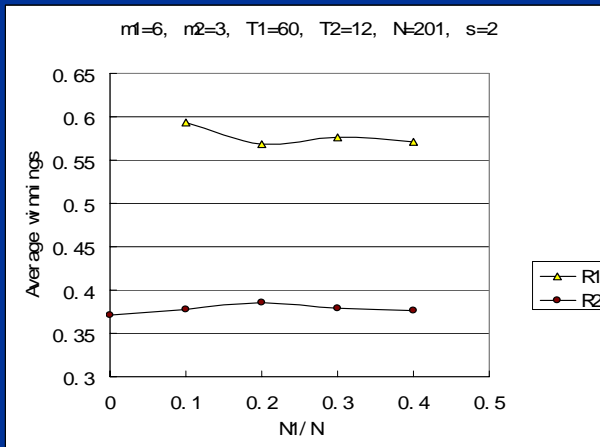


Table 2 correlations of R1, R1 and Vol.2 under the condition of $m1=6$, $m2=3$, $T1=60$, $T2=12$



Correlation	<i>R1</i>	<i>R2</i>	<i>Vol.2</i>
<i>R1</i>	<i>1</i>		
<i>R2</i>	<i>-0.48</i>	<i>1</i>	
<i>Vol.2</i>	<i>0.98</i>	<i>-0.67</i>	<i>1</i>

Average winnings per agent per turn

3.4 Correlation among R1, R2 and Vol.3

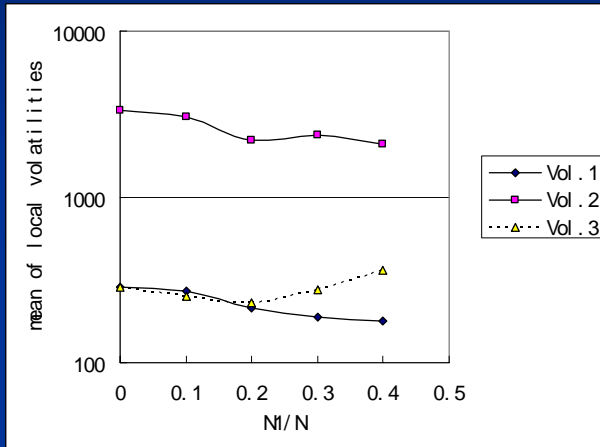
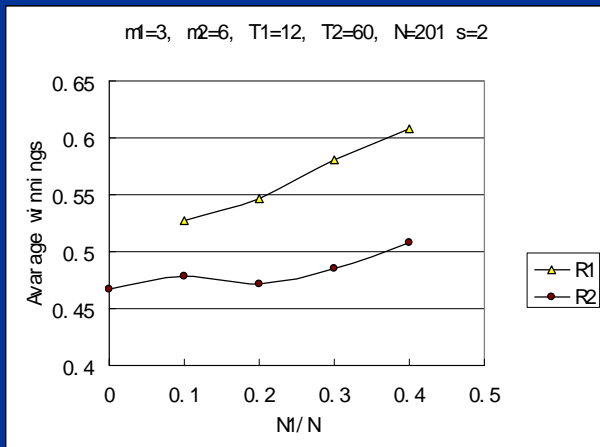


Table 3 correlations of R1, R2 and Vol.3 under the condition of $m1=3$, $m2=6$, $T1=12$, $T2=60$



Correlation	<i>R1</i>	<i>R2</i>	<i>Vol.3</i>
<i>R1</i>	1		
<i>R2</i>	0.87	1	
<i>Vol.3</i>	0.89	0.82	1

Average winnings per agent per turn

4. Design in competing complex systems

- If we want to design a system with both high efficiency of the system and high individual performance, we need to make the agents have different payoffs, the same memory lengths and a relatively large number of agents in group1.

Further reading

- Chengling Gou, *Dynamic Behaviors of Mix-game Model and Its Applications*,
<http://arxiv.org/abs/physics/0504001>
- Chengling Gou, *Agents Play Mix-game*,
<http://arxiv.org/abs/physics/0505112>
- Chengling Gou, *Design in Complex Systems: Individual Performance versus System Efficiency*,
<http://arxiv.org/abs/physics/0505178>

Thanks